YNbO₄-addition on the fracture toughness of ZrO₂(3Y) ceramics

SHENG-DIH YUH, YUANG-CHANG LAI, CHEN-CHIA CHOU* Department of Mechanical Engineering, National Taiwan University of Science and Technology, Taipei, 106, Taiwan, Republic of China E-mail: ccchou@mail.ntust.edu.tw

HSIN-YI LEE

Synchrotron Radiation Research Center, Hsinchu 335, Taiwan, Republic of China E-mail: hylee@alpha1.srrc.gov.tw

Effect of YNbO₄ addition on the fracture toughness and stress-strain characteristics of $ZrO_2(3Y)$ ceramics was investigated using micro-indentation, X-ray diffractometry and in-situ compression-diffraction techniques in the present work. X-ray diffraction patterns show that sintering of YNbO₄ and $ZrO_2(3Y)$ mixture results in formation of a solid solution, and the tetragonality of ZrO₂(3Y) ceramics increases with the content of YNbO₄. The ratio of 002t to 200t peak intensity in X-ray diffraction spectra of the specimens changes significantly after a grinding process at low fractions of $YNbO_4$ (less than 5 mol%) and approaches to a constant value as the content of YNbO₄ is higher than 5 mol%, implying that the addition of YNbO₄ reduces the domain switchability of the ZrO₂(3Y) ceramics. Fracture toughness of modified- $ZrO_2(3Y)$ specimens with the same heat treatment conditions could be greatly enhanced by an appropriate addition of YNbO₄. In addition, stress-strain curves of YNbO₄-modified ZrO₂(3Y) specimens exhibit an extraordinary elastic behavior. Data of in-situ loading-diffraction experiment show that an unidentified stress-induced transformation occurs and the peak intensity varies with the stress conditions. Analysis of the stress-strain characteristics and X-ray diffraction results suggest that the fracture toughness of the specimens cannot be simply attributed to the t-to-m phase transformation. © 2001 Kluwer Academic Publishers

1. Introduction

Since Garvie *et al.* [1,2] firstly realize the potential of utilizing the tetragonal-to-monoclinic (t-to-m) phase transformation of metastable tetragonal zirconia for increasing both strength as well as toughness of the ceramics, the relationship between fracture toughness and phase transformation in zirconia-based ceramics has been studied extensively over the past two decades [3–10].

For partially stabilized zirconia (PSZ) and tetragonal zirconia polycrystals (TZP), the volume change and the shear strain developed in the t-to-m martensitic transformation have been recognized to oppose the opening of the crack, and hence increase the resistance to crack propagation in ceramics. This is the generally accepted toughening mechanism in the zirconia-related materials [1–10]. However, some experimental results indicated that toughening behavior in zirconia-related materials could not be simply interpreted in terms of phase transformation toughening. Ferroelastic domain switching and other behavior have recently been observed and may contribute to the fracture toughness of

some zirconia-related materials [11–24]. For example, Ingel et al. [14, 15] observed that yttria-doped single crystals of partially stabilized zirconia exhibited fracture toughness twice in magnitude as that of fully stabilized crystals at 1100°C. Transformation toughening alone cannot account for this retention of high toughness above the monoclinic-to-tetragonal transition temperature, since the corresponding stress-induced t-to-m transformation has been shown not to be possible above approximately 900°C.¹⁵ Michel *et al.* [16, 17] found the fracture toughness of the tetragonal single crystals of zirconia to be about 6 MPa \cdot m^{1/2} and analysis of fracture surfaces of the crystals by X-ray diffraction also failed to reveal existence of the monoclinic phase, which is not in accordance with the transformation toughening mechanism. This phenomenon is observed by Tsukuma et al. [18] in yttria-doped polycrystalline zirconia as well. The results [11-24] indicate that transformation toughening does not fully explain the observed high toughness of the materials.

Furthermore, Virkar *et al.* [11–13] have observed that ceria-stabilized tetragonal zirconia ceramics exhibit an

increase in the (002) peak intensity and a simultaneous decrease in the (200) peak intensity after surface grinding. Srinivasan et al. [21] and Saiki et al. [22] observed the domains of zirconia single crystals undergoing switching after applying a stress, using an X-ray diffractometry method. Lankford et al. [23] have reported yttria-stabilized zirconia to exhibit two-stage yielding in the stress-strain behavior, yet, no monoclinic phase was present in the yielding process. All these results appear to suggest that the domain switching may probably be an effective toughening mechanism in zirconia-based and related materials. However, in most cases it is difficult to differentiate the effect of phase transformation from that of ferroelastic domain switching on the toughening behavior. In this paper, we report the effect of YNbO4 addition on the phase assemblage, toughness and some intriguing behavior of stress-strain curves of ZrO₂(3Y) modified with YNbO₄ in contrast to previous works [25-27]. An endeavor to differentiate the toughening mechanisms has also been attempted.

2. Experimental

The $YNbO_4$ powders were prepared from Y_2O_3 (99.99%, Research chemicals, USA) and Nb₂O₅ (99.9%, Meldform, UK) by an oxide-mixing method, followed by calcination at 1100°C. The specimen compositions prepared were ZrO₂(3Y) (HSY-3, Daiichi, Japan) with 0 to 20 mol% YNbO₄. The mixtures of $YNbO_4$ and $ZrO_2(3Y)$ were sequentially processed by wet centrifugal ball milling, vacuum drying at 60°C, calcining at 1000°C and ball milling again. The resulting powders were compressed using a cold-isostaticpress under a loading of 270 MPa to form cylindrical pellets or rods. Final specimens were obtained by sintering these pellets from 1350 to 1700°C in air for different periods [28]. X-ray diffraction measurements were made on the specimen surface and interior. To derive data from specimen interior, the specimens were cut slowly into two pieces using a diamond saw and then polished with diamond paste carefully to remove the plastically deformed layer. Phase identifications of as-sintered and fractured surfaces were performed by X-ray diffractometry (DMAX-B, Rigaku, Japan) using Cu K_{α} radiation and the fractions of phases in the materials were estimated employing Howard and Hill's polymorph method [29]. Mechanical property investigations were carried out after the specimens were ground, some were stress-relief heat treated and then polished. Micro-hardness measurements were carried out using a Vickers hardness tester (DVK-1S, Matsuzawa, Japan), and the fracture toughness was determined by micro-indentation technique using the equation recommended by Japanese Industry Standard (JIS R1607, 1995): $K_{\rm IC} = 0.018 (E/H)^{1/2} (P/C)^{1.5}$, where $K_{\rm IC}$ is the fracture toughness in unit MPa $m^{1/2}$; E is the elastic modulus in unit Pa and was measured using a uniaxial compressive loading on a cylinder rod $(\phi = 6 \text{ mm}, \text{ gage length} = 25 \text{ mm})$ with a crosshead speed of 10.0 μ m/min using a dynamic material testing system (MTS 810, USA); H is the Vickers hardness; P is the indentation load in unit N and C is one half of the average length of the four corner cracks of the indent in unit μ m.

In-situ high resolution X-ray diffraction measurements were carried out at the wiggler beamline BL-17B at the Synchrotron Radiation Research Center, Hsinchu, Taiwan. The electron storage ring was operated at energy of 1.5 GeV, and a current of 140-200 mA, which delivered 8.04 KeV X-ray photons with an estimated flux of 10¹⁰ photons/sec for this experiment. The specimens were fixed using a custom designed gripper and then put on a holder of the X-ray diffractometer. The specimens were bonded with a strain gage (Measurements Group, EA-06-250BF-350-option LE, USA) and then compressed uniaxially by a screw wrench. The strain was measured using a strain indicator (Measurements Group, P-3500, USA). In-situ diffraction patterns were obtained from the as-sintered, compressed and released surfaces. Grain size, specimen surface and internal structure of specimens were investigated employing a scanning electron microscope (Hitachi S800, Japan) and a transmission electron microscope (JEOL JEM-2010, Japan) with a double-tilt specimen stage.

3. Results and discussion

X-ray diffraction pattern of the YNbO₄ powder prepared by an oxide-mixing method and calcined at 1100° C is shown in Fig. 1, which shows that the YNbO₄ phase has completely formed (peaks match with JCPDS 23-1468), and some intermediate phases disappear during the sintering process.

X-ray diffraction patterns of the $ZrO_2(3Y)$ specimens, doped with different YNbO₄ contents and sintered at 1600°C for 1 hour, are shown in Fig. 2. It is observed that as the amount of YNbO₄ is smaller than 10 mol %, the specimens exhibit no YNbO₄ peaks after sintering, implying that YNbO₄ has been completely dissolved in $ZrO_2(3Y)$ at the present heat treatment condition. If the content of YNbO₄ is more than 10 mol %, undissolved YNbO₄ can be observed. Fig. 2 also shows that the specimens are mainly the tetragonal and the cubic phases, and the amount of the monoclinic phase is limited.

Relative densities and Vickers hardness of the modified- $ZrO_2(3Y)$ specimens are revealed in Fig. 3.



Figure 1 X-ray diffraction pattern of the YNbO₄ powder prepared by an oxide-mixing method and calcined at 1100°C. All peaks match with JCPDS 23-1468.



Figure 2 X-ray diffraction patterns of ZrO_2 (3Y) specimens with different YNbO₄ contents (a) 0, (b) 5, (c) 10, (d) 15 and (e) 20 mol % sintered at 1600°C for 1 hour. The asterisks indicate YNbO₄ peaks.



Figure 3 The relative density and the Vickers hardness of $ZrO_2(3Y)$ specimens with different YNbO₄ contents sintered at 1600°C for 1 hour.

It shows that the relative density maintains higher than 98% while the Vickers hardness of the specimens show an intriguing tendency, that is, it decreases firstly and then increases as contents of $YNbO_4$ increases, showing a hardness minimum at around 5 mol % $YNbO_4$. Scanning electron micrographs of the specimens are presented in Fig. 4. It can be seen that the addition of $YNbO_4$ promotes the grain growth. Average grain sizes of specimens were calculated and summarized later.

Indentation microcrack of the specimens of $ZrO_2(3Y)$ doped with different $YNbO_4$ contents sintered at 1600°C for 1 hour are shown in Fig. 5. Specimens with 2.5 to 5 mol % $YNbO_4$ show very small

indentation cracks, which suggest that modified $ZrO_2(3Y)$ with a suitable $YNbO_4$ concentration (around 2.5 to 5 mol%) does enhance the fracture toughness of $ZrO_2(3Y)$ effectively.

Two possible toughening mechanisms, domain switching and t-to-m phase transformation, may work in the zirconia-based materials as described in introduction. In order to demonstrate the occurrence of domain switching in the tetragonal phase, the specimens were subjected to grinding process and the X-ray diffraction patterns of the as-sintered and the surface-ground specimens were recorded. Fig. 6 shows the X-ray diffraction peaks associated with 002_t and 200_t planes at 2θ around 34-36° in as-sintered as well as ground specimens of ZrO₂(3Y) doped with different YNbO₄ contents sintered at 1600°C for 1 hour. A sketch of the ratio of peak intensity, $002_t/200_t$, for the specimens before and after grinding is shown in Fig. 7, which implies that grinding induced domain switching occurs for specimens with YNbO₄ content smaller than 7.5 mol %. For specimens with YNbO₄ content higher than 7.5 mol %, domain switching was not observed, suggesting that YNbO4 addition suppress domain switchability of the specimens. At the same time, we measure the phase assemblage of the fracture surface of specimens, as shown in Fig. 8. The results show that the tetragonal phase of the specimen containing 2.5 mol % YNbO4 has transformed to the monoclinic phase in a large amount, while the specimen containing 10 mol % YNbO4 almost shows no monoclinic phase on the fracture surface. This suggests that YNbO₄ addition suppress not only domain switching but also the t-to-m transformation of the specimens, as the specimens possess YNbO₄ content higher than 7.5 mol %.

Summary of characteristics of the specimens was drawn as a function of different $YNbO_4$ content, shown in Fig. 9. Variations of the fracture toughness is observed as the curve "K" in Fig. 9, which shows that the fracture toughness of the specimen with 2.5 mol % $YNbO_4$ is nearly 2.5 times higher than that without $YNbO_4$ addition under identical preparation conditions. The fraction of the tetragonal phase and the grain size were calculated and shown by curves "t" and "G" in Fig. 9, respectively. The c/a ratio, i.e, the tetragonality, calculated from Fig. 2 for the tetragonal phase of the specimens approaches to a saturation value, as $YNbO_4$ content increases, as shown by the curve "T" in Fig. 9.

Aliovalent cation dopants are generally believed to substitute for Zr ions in the cation network, creating oxygen vacancies for charge compensation [30]. The ensuing lattice distortion by oxygen vacancies associated with Zr provides stability to the tetragonal and cubic phases of zirconia [31]. However, the number of such oxygen vacancies increases during stabilization process, which consequently causes the tetragonality of zirconia to decrease [30]. On the other hand, in the solid solution of the tetragonal zirconia with YNbO₄, Y adopts a YO₈ structure with a bond length of 2.32 Å and is not associated with oxygen vacancies, while Nb adopts a NbO₄ structure with a bond length of 1.90 Å. This is shorter than the Zr-O_I distance of 2.10 Å. The strong Nb-O coordination thus



0 mol %

5 mol %



10 mol %

15 mol %

Figure 4 Scanning electron micrographs of the specimens with different YNbO4 contents. The specimens were sintered at 1600°C for 1 hour.





Figure 5 Indentation microcrack development in specimens with different YNbO4 contents sintered at 1600°C for 1 hour.



Figure 6 Expended XRD patterns for 002_t and 200_t peak intensity at $2\theta = 34-36^\circ$ for $ZrO_2(3Y)$ specimens with different YNbO₄ contents. The specimens were sintered at 1600° C for 1 hour.

increases the bonding disparity between Zr-O layers, consequently increasing the tetragonality [31]. This is consistent with the present result shown by curve "T" in Fig. 9. Furthermore, it has been shown that the fracture toughness increases with increase in tetragonality in the Nb₂O₅-ZrO₂ system [32, 33]. This was explained by arguing that Nb⁵⁺ combines with oxygen interstitial in ZrO₂ during formation of Nb₂O₅ solid solution with ZrO₂, which reduces the concentration of the oxygen vacancies and makes the tetragonal phase unstable. It

means that phase transformability from tetragonal to monoclinic increases with addition of Nb, and thus the fracture toughness enhancement appears to be simply related to a phase transformation mechanism. However, by observing Figs 7 and 9, the fracture toughness of the YNbO₄-doped ZrO₂(3Y) specimens decreases as the c/a ratio increases for specimens with YNbO₄ content higher than 5 mol %. This may be due to the chemical composition modification of the specimens showing constant oxygen vacancy concentration, which is

Figure 7 Intensity ratio of the peaks $002_t/200_t$ for ZrO₂(3Y) specimens with different YNbO₄ contents before and after grinding. The specimens were sintered at 1600°C for 1 hour.

Figure 8 The changes of the diffraction peak before and after fracture of the $ZrO_2(3Y)$ specimen doped with 2.5 and 10 mol % YNbO₄. The specimens were sintered at 1600°C for 1 hour.

different from that of the Nb_2O_5 -ZrO₂ system, and may be attributed to the stabilization of the tetragonal phase in the present material system.

Fracture toughness of a tetragonal zirconia polycrystal is strongly dependent on the grain size [34]. The tetragonal phase becomes easier to transform when grain size of a specimen increases. Contribution of t-to-m transformation to fracture toughness contribution at a constant temperature therefore increases [35]. To verify the grain size and the composition homogeneity effects, $ZrO_2(3Y)$ specimens doped with different YNbO₄ contents sintered at 1600°C for 10 hours were investigated. Again, we observe that the addition of YNbO₄ promotes the grain growth. The fracture toughness of the speci-

Figure 9 Variations in fracture toughness, tetragonality, fraction of the tetragonal phase and grain size for specimens with different YNbO₄ contents. The specimens were sintered at 1600° C for 1 hour.

Figure 10 Fraction of the monoclinic phase, fracture toughness and grain size for $ZrO_2(3Y)$ specimens (as-sintered) with different YNbO₄ contents sintered at 1600°C for 10 hours.

mens and the corresponding fraction of the monoclinic phase are shown in Fig. 10. The $ZrO_2(3Y)$ specimen show a prominent increase in fracture toughness due to the grain size effect on transformability. Fig. 10 provides an interesting result indicating that tto-m transformation may not be the only toughening mechanism for the specimens. That is, although fraction of the monoclinic phase in the 5 mol% YNbO₄ specimen is as high as 60%, the specimen still exhibits a nearly highest value of the fracture toughness. On the other hand, as 2.5 mol% YNbO₄ was added in the specimen, a large amount of the monoclinic phase was introduced but a rapid drop of the fracture toughness of the specimen was observed. Intriguingly, grain size of the specimen with 5 mol%

Figure 11 An axial stress-strain curve of ZrO₂(3Y)-5 mol%YNbO₄ specimens sintered at 1600°C for 1 hour under a compression test showing hysteresis loops without permanent strain.

YNbO₄ is larger than that of the specimen with 2.5 mol% YNbO₄. This suggests that YNbO₄ addition with amounts smaller than or around 5 mol% not only greatly enhance grain growth, but also modify the t-to-m transformation characteristics. The tetragonal phase of a specimen may have transformed into the monoclinic phase in a large amount, but the fracture toughness of the specimens does not necessarily decay. This high toughness of the ZrO₂(3Y) specimen with 5 mol% YNbO₄ can not be simply explained by a t-to-m phase transformation mechanism, since a large amount of the tetragonal phase have transformed into the monoclinic phase. Origin of this high toughness therefore may probably be attributed to domain switching or other mechanisms. In addition, when the YNbO₄ addition is higher than 7.5 mol %, increasing in tetragonality of the specimens suppresses the phase transformability and makes toughness of the YNbO₄doped specimens decrease, indicating that phase transformation induced volume change and therefore the compressive stress do play a role in toughness enhancement.

Enhancement of the energy absorbing capability of a brittle material can be observed by the increase of its ductility. Fig. 11 shows the stress-strain curves of a cylindrical specimen of ZrO₂(3Y)-5 mol% YNbO₄ sintered at 1600°C for 1 hour in a compression experiment under a loading of 415 MPa. Intriguingly, the compressed specimen exhibited a hysteresis loop at the axial direction in the stress-strain curve during loading-unloading process. The strain recovers completely after unloading. This kind of pseudoelastic behavior is ordinarily attributed to a reversible stressinduced-transformation or a ferroelastic behavior of the materials [36]. Materials containing a reversible stressinduced phase transformation show large pseudoelastic strains due to a structural change during a phase transition [36]. Ferroelastic materials often exhibit high elastic deformation and often contain movable domain

Figure 12 The variation of the diffraction peaks under *in-situ* uni-axial compression loading of the ZrO₂-5 mol%YNbO₄ specimen sintered at 1600°C for 1 hr. (a) initial state, (b) 1000 $\mu\epsilon$, (c) 2000 $\mu\epsilon$ and (d) released condition.

boundaries which soften the materials [37–39]. The area enclosed by the hysteresis loops shown in Fig. 11, could be the mechanical energy stored in the material in a loading cycle due to either a ferroelastic behavior [11] or a stress-induced-transformation [36].

To verify either a ferroelastic behavior or a stressinduced-transformation in the material, an *in-situ* high resolution diffractometry for uniaxial compression experiments using synchrotron radiation was conducted. The intensity variations of diffraction patterns during loading and unloading procedures under a uniaxial compression of rectangular specimen ZrO₂(3Y) doped with 5 mol % YNbO₄ sintered at 1600°C for 1 hour are shown in Fig. 12. At the initial loading-free condition, two peaks exist between 002_t and 200_t . One of these two peaks is cubic phase 200c which is originally subsistent in YNbO₄-doped ZrO₂(3Y) specimens, and the other is an unidentified phase which was not reported to exist in $ZrO_2(3Y)$ specimens. The formation of this unidentified phase in the present material system is because of the YNbO₄-addition. Intriguingly, the peak intensity of this phase varies with the stress condition under the condition of no apparent changes in intensity of the tetragonal peaks of 002_t and 200_t . That is, the result indicates that an stress-induced transformation rather than t-to-m transformation or a stress-induced domain switching occur in the present material system.

In addition to the well-known cubic, tetragonal and monoclinic polymorphs of the zirconia, this extra phase can be confirmed by transmission electron microscopy. Fig. 13 shows the morphology and the corresponding diffraction pattern of a specimen of $ZrO_2(3Y)$ doped with 5 mol % YNbO₄ sintered at 1600°C for 1 hour. Note that around the principal reflections, which were analyzed to be the monoclinic twins and the tetragonal

Figure 13 TEM micrograph showing (a) a bright field image with complicated internal structures, (b) the corresponding diffraction pattern and (c) indices showing a zone axis of [010] for the tetragonal phase, $[01\overline{2}]$ for the monoclinic phase and some spots for undefined (indicated by solid circle) phases.

phase, fine and weak extra spots were observed. These extra spots can not be ascribed to the cubic, the tetragonal and the monoclinic phases and preliminary analyses indicate that the phase may probably be the orthorhombic and/or rhombohedral phases, but the peak positions do not match very well with those reported in the previous works [40–42].

4. Conclusions

The effect of $YNbO_4$ addition on fracture toughening of $ZrO_2(3Y)$ ceramics was investigated. The main results are summarized as follows:

1. Sintering of $YNbO_4$ and $ZrO_2(3Y)$ mixture results in a solid solution with $YNbO_4$ content smaller

than 10 mol%, and tetragonality of $ZrO_2(3Y)$ ceramics increases with the content of $YNbO_4$. Addition of $YNbO_4$ promotes grain growth of the specimens and stabilizes the tetragonal phase effectively.

2. The intensity of $(002)_t$ and $(200)_t$ peaks changes greatly at low fractions of YNbO₄ (0 and 2.5 mol%) after grinding, while it saturates with further increase in the content of YNbO₄. Phase assemblage of the fracture surface of specimens shows that the t-to-m transformation occurs more easily for the specimen containing lower content of YNbO₄. The result implies that addition of YNbO₄ reduces the domain switchability and the phase transformability of the ZrO₂(3Y) ceramics.

3. Fraction of the monoclinic phase in the $ZrO_2(3Y) + 5 mol \% YNbO_4$ specimen sintered at 1600°C for 1 hour is as high as 60%, the specimen still exhibits a nearly highest value of the fracture toughness. On the other hand, as 2.5 mol % YNbO₄ was added in the specimen, a large amount of the monoclinic phase was introduced but a rapid drop of the fracture toughness of the specimen was observed. Intriguingly, grain size of the specimen with 5 mol% YNbO₄ is larger than that of the specimen with 2.5 mol % YNbO₄. This suggests that YNbO₄ addition with amounts smaller than or around 5 mol % not only greatly enhance grain growth, but also modify the t-to-m transformation. The tetragonal phase of a specimen may have transformed into the monoclinic phase in a large amount, but the fracture toughness of the specimens does not necessarily decay.

4. Fracture toughness of modified- $ZrO_2(3Y)$ specimens with the same heat treatment conditions could be greatly enhanced by an appropriate addition of YNbO₄. In addition, stress-strain curves of YNbO₄-modified $ZrO_2(3Y)$ specimens exhibit an extraordinary elastic behavior. Data of *in-situ* compression-diffraction experiment show that an unidentified stress-induced transformation occurs and the peak intensity varies with the stress conditions. Analysis of the stress-strain characteristics and X-ray diffraction results suggest that the fracture toughness of the specimens can not be simply attributed to the t-to-m phase transformation.

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